

SEAKEEPING NUMERICAL ANALYSIS IN IRREGULAR WAVES OF A CONTAINERSHIP

Carmen GASPAROTTI, Eugen RUSU

University of Galati, ROMANIA

carmen.gasparotti@ugal.ro

ABSTRACT

In the present work, a seakeeping analysis of a containership of 139,96m length, is performed. The study includes the linear seakeeping analysis, coupled heave and pitch motions, uncoupled roll motion, in irregular waves, heading angle $0 \div 360$ deg., with Pierson-Moskowitz wave power density spectrum. The numerical seakeeping analyses are carried on with an original DYN_OSC program code based on linear seakeeping method and statistical short term prediction response method. Taking into account the specific limits of seakeeping criteria, the dynamic response statistical polar diagrams are obtained for each motion degree and the cumulative one, pointing out the influence of the ship speed and heading angle for seakeeping assessment.

Keywords: numerical seakeeping analysis, dynamic response, seakeeping criteria

1. INTRODUCTION

An analysis of seakeeping characteristics of a ship moving in regular waves and irregular waves actually involves the analysis of ship behaviour in waves [1].

The evaluation of seakeeping performance of a ship largely depends on the environmental conditions and defined criteria and this is the main reason that any comparison related to the ship speeds, the influence of heading angles, loading conditions, etc.. is a complex problem.

Seakeeping analysis is essentially a three part problem [2]:

1. estimation of the likely environmental conditions to be encountered by the vessel,
2. prediction of the response characteristics of the vessel,
3. specification of the criteria used to assess the vessel's seakeeping behaviour. This also defines the way in which the performance of different vessels is compared.

Evaluation of seakeeping performance of a ship shall be based on its oscillations in different states of the sea that is expected to encounter during its lifetime. The procedure starts with the predicting hydrodynamic characteristics of the ship response for several speeds and heading angles. In irregular waves, short-term and long term distributions can be used to estimate the most probable maximum values of responses.

Magnitude increase movement in varying degrees of severity can then be predicted, using wave spectra representative for the selected operational sea areas. Usually, the sea

state is described by a theoretical wave spectrum [3]. Finally, the capacity of the ship can be estimated on the basis of probability of the remaining ship movements within acceptable limits.

In this context, the objective of the present work is to analyse the ship speed and heading angle influence on maximum RMS heave, pitch, roll motion and acceleration amplitudes. The numerical seakeeping analyses based on linear seakeeping method and statistical short term prediction response method is presented in section 2 of the work.

Table 1 presents the main characteristics of the ship.

Table 1. Simplified test ship main characteristics

L [m]	139.96	Δ [t]	17974.5
B [m]	21.8	J_x [t m ²]	1067775
H [m]	9.5	J_y [t m ²]	25222622
d [m]	7.335	I_y [m ⁴]	3376696
c_B	1	A_w [m ²]	2637.79
H_{fore} [m]	6	$N_{sections}$	43
F_{fore} [m]	2.5	μ [deg.], $\delta\mu$	0÷360, 15
h_0 [m]	3.418	u_s [knots]	0, 5, 10, 15, 19
z_g [m]	5.5	T_ζ [s]	7.40633
$x_{g,B,F}$ [m]	69.48	T_θ [s]	7.34945
g [m/s ²]	9.81	T_ϕ [s]	9.60724
ρ_{water} [t/m ³]	1.025	symmetric CL & amidships	

2. THEORETICAL BACKGROUND

This study refers to a containership and it includes a linear seakeeping analysis in irregular waves, coupled heave and pitch motions, uncoupled roll motion, heading angle $0 \div 360$ deg., with ISSC wave power density spectrum. The seakeeping analysis from this study is carried on under the following hypotheses [4]:

- the excitation source is wave Airy model;
- the motion equations are linearized;
- the ship-sides are considered vertical;
- the motions amplitudes are considered small;
- the Lewis based hydrodynamic coefficients;
- the strip theory based hydrodynamic forces [5].

In order to meet short-term statistical parameters, the authors need to know wave spectral density function. This function must be characteristic of the sea area where the ship will sail, which is not always possible, in this sense using known standard wave spectra, accepted in ocean engineering.

Spectral density functions of the dynamic response to variations of the ship have the expressions[6]:

- vertical (heave):

$$S_z(\omega, \mu) = H_z^2(\omega, \mu) \cdot \Phi_{\zeta_v \zeta_v}(\omega) = RAO_z(\omega, \mu) \cdot \Phi_{\zeta_v \zeta_v}(\omega) \quad (1)$$

- pitch (pitch):

$$S_\theta(\omega, \mu) = H_\theta^2(\omega, \mu) \cdot \Phi_{\zeta_v \zeta_v}(\omega) = RAO_\theta(\omega, \mu) \cdot \Phi_{\zeta_v \zeta_v}(\omega) \quad (2)$$

- roll (roll):

$$S_\phi(\omega, \mu) = H_\phi^2(\omega, \mu) \cdot \Phi_{\zeta_v \zeta_v}(\omega) = RAO_\phi(\omega, \mu) \cdot \Phi_{\zeta_v \zeta_v}(\omega) \quad (3)$$

Moments of the spectral density function of the dynamic response to fluctuations of the ship are:

$$\begin{aligned} m_{0z}(\mu) &= \int_0^{\omega_{\max}} S_z(\omega, \mu) d\omega; & m_{0\theta}(\mu) &= \int_0^{\omega_{\max}} S_{\theta}(\omega, \mu) d\omega; & m_{0\varphi}(\mu) &= \int_0^{\omega_{\max}} S_{\varphi}(\omega, \mu) d\omega \\ m_{4z}(\mu) &= \int_0^{\omega_{\max}} \omega^4 S_z(\omega, \mu) d\omega; & m_{4\theta}(\mu) &= \int_0^{\omega_{\max}} \omega^4 S_{\theta}(\omega, \mu) d\omega; & m_{4\varphi}(\mu) &= \int_0^{\omega_{\max}} \omega^4 S_{\varphi}(\omega, \mu) d\omega \end{aligned} \quad (4)$$

Based on the spectral moments, the most probable amplitude of the motion and acceleration to the oscillation $a_{\text{mp}} = \text{RMS}$ (root mean square) are calculated [6]:

• vertical :

$$\text{RMS}_z(\mu) = \sqrt{m_{0z}(\mu)} \quad (5)$$

$$\text{RMSac}_z(\mu) = \sqrt{m_{4z}(\mu)}$$

$$\text{RMS}_{z_{\max}} = F + F_s - Z_{pv\theta} \quad (6)$$

$$\text{RMSac}_{z_{\max}} = 0.1 \cdot g$$

• pitch :

$$\text{RMS}_{\theta}(\mu) = \sqrt{m_{0\theta}(\mu)}$$

$$\text{RMSac}_{\theta}(\mu) = \sqrt{m_{4\theta}(\mu)}$$

$$\text{RMSac}_{\theta_{pv}}(\mu) = \frac{L}{2} \cdot \text{RMSac}_{\theta}(\mu)$$

$$\text{RMS}_{\theta_{\max}} = 3^0 = 0.052 \text{ rad} \Rightarrow Z_{pv\theta} = \frac{L}{2} \cdot \text{RMS}_{\theta_{\max}}; \quad \text{RMSac}_{\theta_{pv \max}} = 0.15 \cdot g \quad (7)$$

• roll :

$$\text{RMS}_{\varphi}(\mu) = \sqrt{m_{0\varphi}(\mu)}$$

$$\text{RMSac}_{\varphi}(\mu) = \sqrt{m_{4\varphi}(\mu)}$$

$$\text{RMSac}_{\varphi_{sb}}(\mu) = \frac{B}{2} \cdot \text{RMSac}_{\varphi}(\mu)$$

$$\text{RMS}_{\varphi_{\max}} = 6^0 = 0.105 \text{ rad}$$

$$\text{RMSac}_{\varphi_{sb \max}} = 0.15 \cdot g \quad (8)$$

Table 2 presents the limit seakeeping criteria for the containership.

Tabel 2 Limit seakeeping criteria

$\text{RMS}_{z_{\max}} = F + F_s - z_{pv}$	1.22	m	not be flooded the deck at the bow	
$\text{RMSac}_{z_{\max}}$	0.1	*g		
$\text{RMS}_{\theta_{\max}}$	2	gr	0.035	rad
$\text{RMSac}_{\varphi_{pv \max}}$	0.15	*g	$L/2$ [m]	69.98
$\text{RMS}_{\varphi_{\max}}$	6	gr	0.105	rad
$\text{RMSac}_{\varphi_{sb \max}}$	0.15	*g	$B/2$ [m]	10.9

Based on limit values RMS_{\max} , RMSac_{\max} , polar diagrams $h_{1/3 \max} = f(\mu, u_s, \text{mot.})$ and Beaufort $B_{\max}(\mu, y)$, for several ship speeds u_s , are determined.

Relevant parameters that characterize the behavior of the ship are forecasting as response spectrum variance functions, that depend on the sea state energy spectrum and the transfer functions of the ship. In the study of seakeeping, the correct selection of wave spectrum for a particular seaway is essential [7].

The first step is to calculate the transfer functions of the ship response to coupled heave (3) and pitch (5) oscillations and uncoupled roll oscillations (4). They took into account a step of 15 degree between the ship and wave main directions, resulting in 13 headings. The transfer functions include the absolute ship motions and vertical, lateral and roll accelerations.

Determination of the response spectrum and statistical quantities to the dynamic analysis of the short-term dynamic response (3 heave, 5 pitch, 4 roll) was performed with the following calculation modules, which take into account of the correction spectra depending on encountering ship-wave equivalent circular frequency [6]:

- HZ35u (DYN_OSC) – calculation module of the transfer functions for coupled heave and pitch dynamic response;
- HR44u (DYN_OSC) – calculation module of the transfer functions for uncoupled roll dynamic response.

In order to calculate the transfer functions for the coupled heave (3) and pitch (5) oscillations and uncoupled roll oscillations (4) have considered the following cases:

- μ heading angle between the ship and wave main direction [degree]= 0, 15, 30, 45, 60, 75, 90, 105, 120, 135, 150, 165, 180;
- us ship speed [Nd]= 0, 5, 10, 15, 19 (0; 2.572; 5.144; 7.714; 9, 7736; [m/s]).

When calculating the statistical significant parameters $a_{1/3}=2 \cdot \text{RMS}$ of the amplitude and acceleration of the ship motion, the following programs have been used:

- SH13_33U (DYN_OSC) to the heave oscillations, resulting the folder SHIP.AS3;
- SH13_55U (DYN_OSC) to the pitch oscillations, resulting the folder SHIP.AS5;
- SH13_44U (DYN_OSC) to the roll oscillations, resulting the folder SHIP.AS4.

In addition for the roll, oscillations were also introduced as input data; initial transverse metacentric height h_0 and roll mass moment of inertia

$$J_x = \Delta \cdot B^2 / 8. \quad (9)$$

$$\omega_e = \omega - k \cdot u_s \cdot \cos \mu \quad (10)$$

$$k = \frac{\omega^2}{g} \quad (10b)$$

where: ω_e = encountering ship-wave equivalent circular frequency [rad/s]; ω = wave frequency [rad/s]; u_s = ship speed [m/s]; $u_s = v \times 0.5144$; v [Nd], g = gravity acceleration [m/s^2], μ = heading angle between the ship and wave main direction [degree], k = wave number [1/m].

The irregular wave Pierson-Moscowitz power density function input spectrum [6], used in this study, has the following expression:

$$E_{PM}(f) = \frac{\alpha g^2}{(2\pi)^4 f^5} e^{-0.74 \left(\frac{g}{2\pi U_{19.5} f} \right)^4} \quad (11)$$

where $E_{PM}(f)$ - spectrum energy ($\text{m}^2 \cdot \text{s}$ or m^2/Hz), f - wave frequency (Hz), $U_{19.5}$ - wind speed (m/s) at 19.5 m over the sea surface, g - gravity acceleration (m/s^2), α - adimensional coefficient, $\alpha = 0.0081$.

From the PM spectrum data analysis, it was carried out the following equation:

$$f_p = 0.877 \frac{g}{2\pi U_{19.5}} \quad (12)$$

Equation (12) permits to calculate m_0 (the mean square of the spectrum) and from this results:

$$H_{m0} = 0.04c_p^{-2} \quad (13)$$

3. NUMERICAL ANALYSIS

For the ship presented in Table 1, the numerical seakeeping analysis results are the following.

Figures.1-5a-c present heave, pitch and roll transfer functions H_{Z3} [m/m], H_{T5} [m/m], H_{R4} [rad/m]. Figures. 6-8a-c present polar diagrams $h_{1/3max}$, B_{max} .

Tables 3-7 present the seakeeping numerical results for polar diagrams, with the limit seakeeping criteria from Table 2.

Tabel. 3 Cumulative limit $h_{1/3}, B_{max} u_s=0$ [kts]

us=0	Short Time Prediction			Polar Diagram	
	33	55	44		
μ	heave	pitch	roll	$h_{1/3max}$	Beaufort
0	8.576	7.537	12.000	7.537	9.17
15	8.444	7.489	12.000	7.489	9.14
30	8.056	7.365	12.000	7.365	9.08
45	7.423	7.275	5.514	5.514	7.95
60	6.535	8.160	3.679	3.679	6.59
75	4.797	12.000	3.143	3.143	6.12
90	3.711	12.000	3.002	3.002	5.99
105	4.665	12.000	3.151	3.151	6.12
120	6.452	8.806	3.710	3.710	6.62
135	7.370	7.637	5.701	5.701	8.07
150	8.020	7.611	12.000	7.611	9.20
165	8.411	7.682	12.000	7.682	9.23
180	8.543	7.714	12.000	7.714	9.25

180 ÷ 360 deg. same as for 180 ÷ 0 deg. due sym
Limit values according to seakeeping criteria are:

$$h_{1/3max}=3.002\div 7.714 \text{ m}; B_{max}=5.99\div 9.25.$$

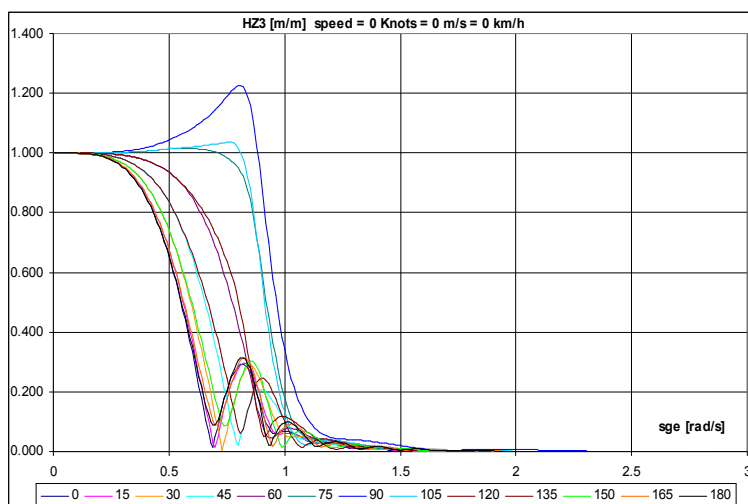


Fig. 1a. Heave transfer function H_{Z3} [m/m], $u_s=0$ [kts]

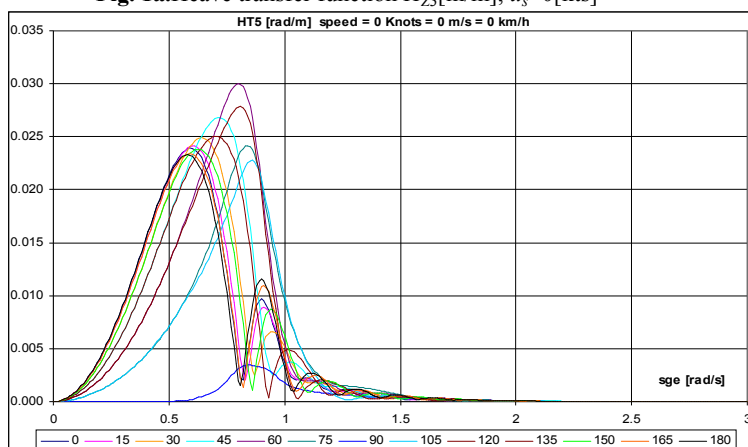


Fig. 1b. Pitch transfer function H_{T5} [m/m], $u_s=0$ [kts]

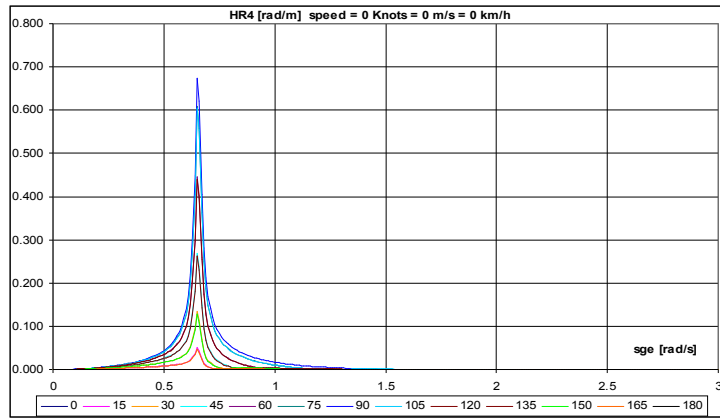


Fig. 1c. Roll transfer function $H_{Rd}[m/m]$, $u_s=0[kts]$

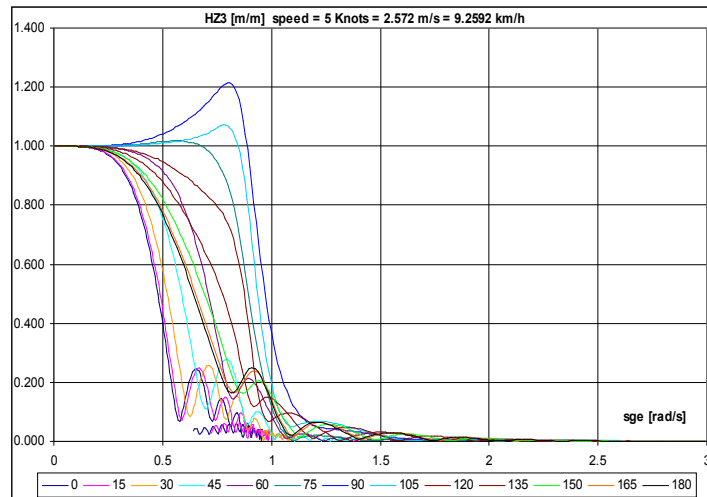


Fig. 2a. Heave transfer function $H_{Z3}[m/m]$, $u_s=5[kts]$

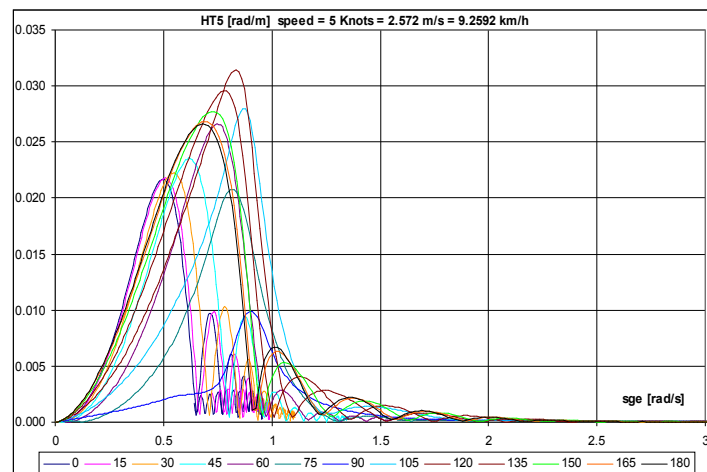


Fig. 2b. Pitch transfer function $H_{T5}[m/m]$, $u_s=5[kts]$

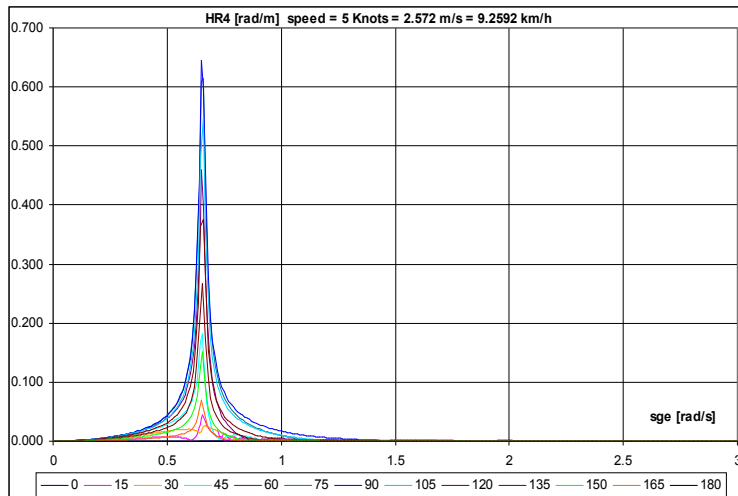


Fig. 2c. Roll transfer function H_{R4} [m/m], $u_s=5$ [kts]

Tabel.4 Cumulative limit $h_{1/3}$, B_{max} $u_s=5$ [kts]

Short Time Prediction		Polar Diagram			
$u_s = 5$	33	55	44		
μ	heave	pitch	roll	$h_{1/3max}$	Beaufort
0	8.491	8.274	12.000	8.274	9.52
15	8.357	8.254	12.000	8.254	9.51
30	7.966	8.253	12.000	7.966	9.37
45	7.319	8.493	12.000	7.319	9.06
60	6.452	10.460	3.285	3.285	6.24
75	5.210	12.000	2.888	2.888	5.85
90	3.683	12.000	3.034	3.034	6.02
105	4.362	12.000	3.462	3.462	6.40
120	6.208	7.260	4.240	4.240	7.07
135	7.320	6.718	5.834	5.834	8.15
150	7.995	6.819	12.000	6.819	8.77
165	8.401	6.960	12.000	6.960	8.86
180	8.535	7.014	12.000	7.014	8.89

180 ÷ 360 deg. same as for 180 ÷ 0 deg. due sym

Limit values according to seakeeping criteria are: $h_{1/3max}=2.888\div 8.274$ m; $B_{max}=5.85\div 9.52$.

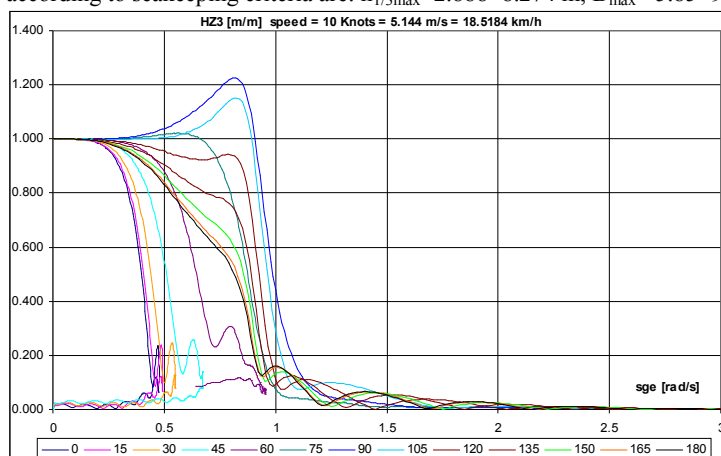


Fig. 3a. Heave transfer function H_{Z3} [m/m], $u_s=10$ [kts]

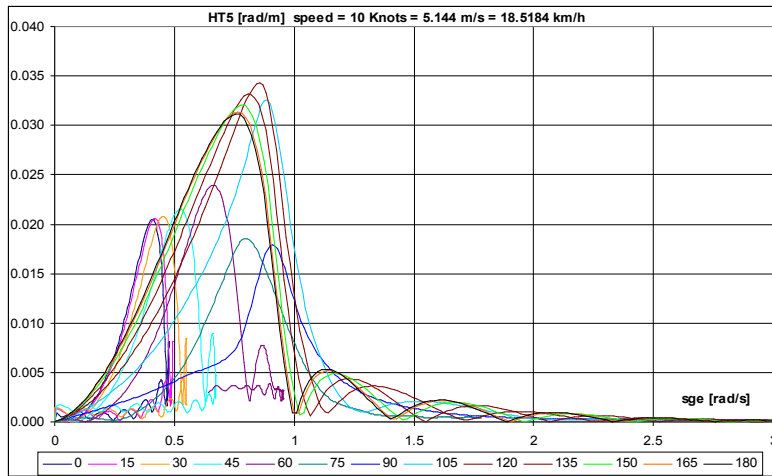


Fig. 3b. Pitch transfer function H_{T5} [m/m], $u_s=10$ [kts]

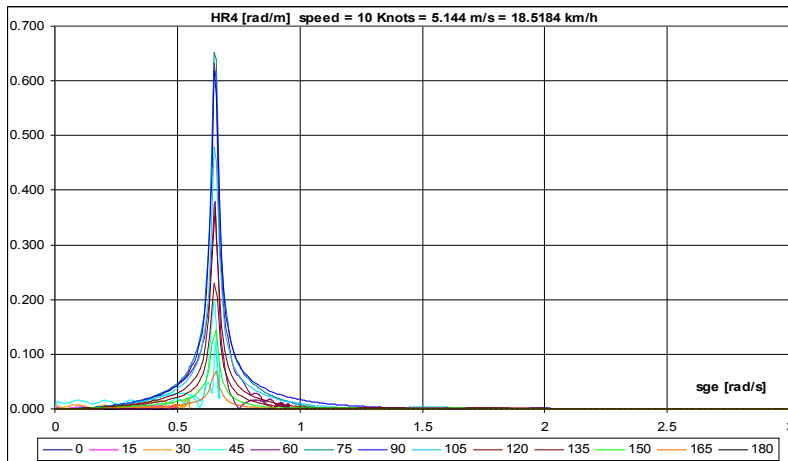


Fig. 3c. Roll transfer function H_{Z3} [m/m], $u_s=10$ [kts]

Tabel.5 Cumulative limit $h_{1/3}$, B_{max} $u_s=10$ [kts]

Short Time Prediction		Polar Diagram			
$u_s=10$	33	55	44		
μ	heave	pitch	roll	$h_{1/3max}$	Beaufort
0	8.411	8.860	12.000	8.411	9.58
15	8.281	8.873	12.000	8.281	9.52
30	7.882	8.942	12.000	7.882	9.33
45	7.240	9.937	12.000	7.240	9.02
60	6.340	12.000	3.232	3.232	6.20
75	5.363	12.000	2.608	2.608	5.50
90	3.508	12.000	3.064	3.064	6.05
105	3.966	9.397	3.764	3.764	6.67
120	5.038	6.399	4.746	4.746	7.42
135	6.262	6.208	6.416	6.208	8.39
150	7.326	6.348	11.968	6.348	8.47
165	8.020	6.488	12.000	6.488	8.56
180	8.246	6.540	12.000	6.540	8.59

180 ÷ 360 deg. same as for 180 ÷ 0 deg. due sym

Limit values according to seakeeping criteria are: $h_{1/3max}=2.608\div 8.411$ m; $B_{max}=5.50\div 9.58$

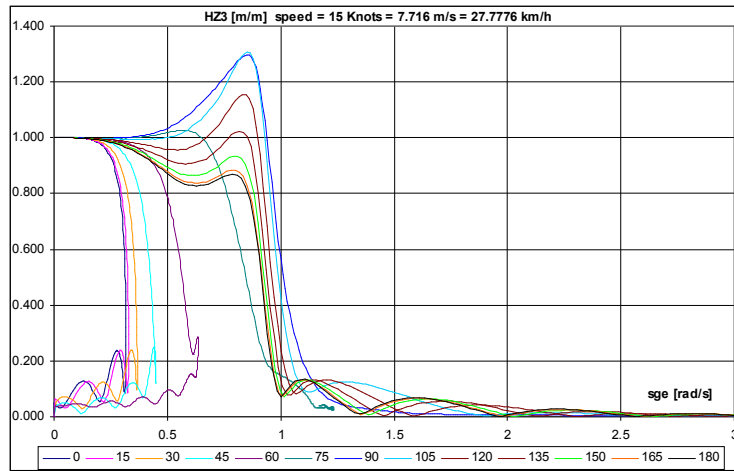


Fig. 4a. Heave transfer function H_{Z3} [m/m], $u_s=15$ [kts]

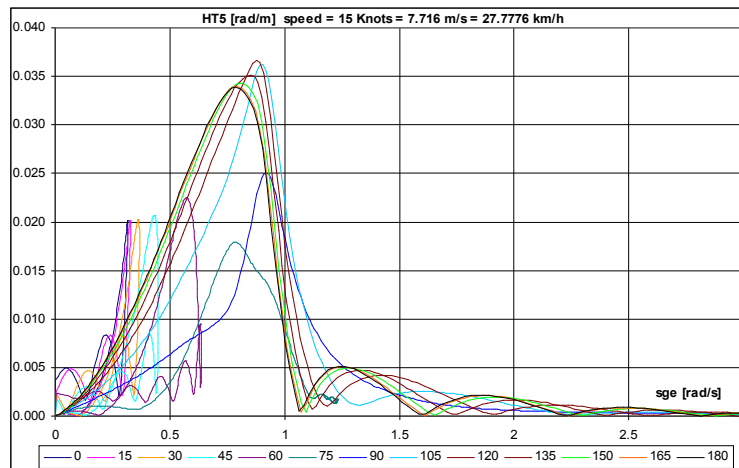


Fig. 4b. Pitch transfer function H_{T5} [rad/m], $u_s=15$ [kts]

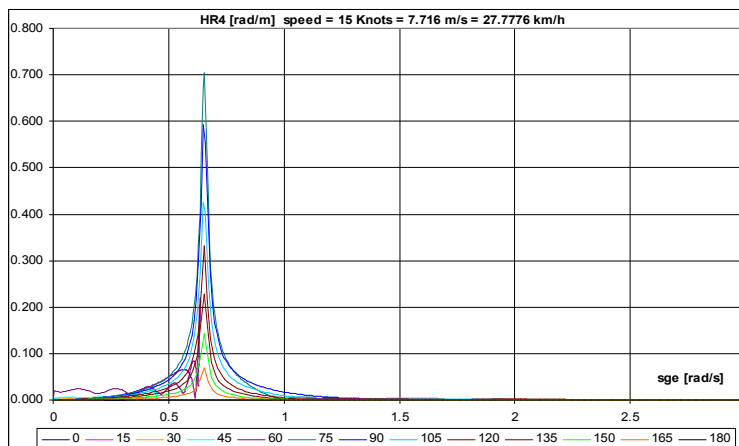


Fig. 4c. Roll transfer function H_{R4} [rad/m], $u_s=15$ [kts]

Table 6. Cumulative limit $h_{1/3}, B_{max}$ $u_s=15$ [kts]

Short Time Prediction			Polar Diagram		
$u_s=15$	33	55	44		
μ	heave	pitch	roll	$h_{1/3max}$	Beaufort
0	8.326	9.166	12.000	8.326	9.54
15	8.216	9.564	12.000	8.216	9.49
30	7.825	10.078	12.000	7.825	9.30
45	7.134	9.260	12.000	7.134	8.96
60	6.273	12.000	12.000	6.273	8.43
75	5.268	12.000	2.294	2.294	5.11
90	3.201	12.000	3.094	3.094	6.07
105	3.562	6.098	4.077	3.562	6.49
120	4.279	5.342	5.265	4.279	7.10
135	4.979	5.595	7.038	4.979	7.58
150	5.543	5.909	11.809	5.543	7.97
165	5.903	6.123	12.000	5.903	8.19
180	6.025	6.199	12.000	6.025	8.27

Table 7. Cumulative limit $h_{1/3}, B_{max}$ $u_s=19$ [kts]

Short Time Prediction			Polar Diagram		
$u_s=19$	33	55	44		
μ	heave	pitch	roll	$h_{1/3max}$	Beaufort
0	8.291	9.423	12.000	8.291	9.53
15	7.909	8.923	12.000	7.909	9.34
30	7.599	9.422	12.000	7.599	9.20
45	7.155	12.000	12.000	7.155	8.98
60	6.246	12.000	12.000	6.246	8.41
75	5.175	12.000	2.007	2.007	4.59
90	2.907	12.000	3.118	2.907	5.87
105	3.300	5.018	4.306	3.300	6.26
120	3.929	4.919	5.673	3.929	6.81
135	4.488	5.243	7.649	4.488	7.24
150	4.919	5.555	12.000	4.919	7.54
165	5.184	5.759	12.000	5.184	7.72
180	5.274	5.830	12.000	5.274	7.78

180 ÷ 360 deg. same as for 180 ÷ 0 deg. due sym
 Limit values according to seakeeping criteria are:
 $h_{1/3max}=2.294\div 8.326$ m; $B_{max}=5.11\div 9.54$

180 ÷ 360 deg. same as for 180 ÷ 0 deg. due sym
 Limit values according to seakeeping criteria are:
 $h_{1/3max}=2.007\div 8.291$ m; $B_{max}=4.59\div 9.53$

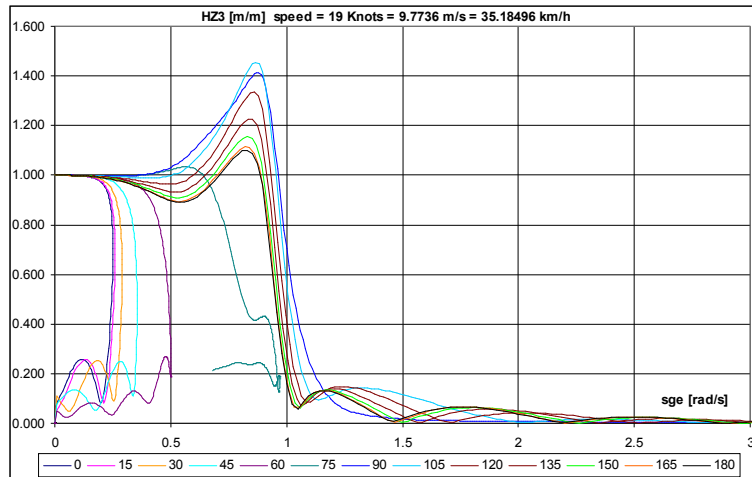


Fig. 5a. Heave transfer function H_{Z3} [m/m], $u_s=19$ [kts]

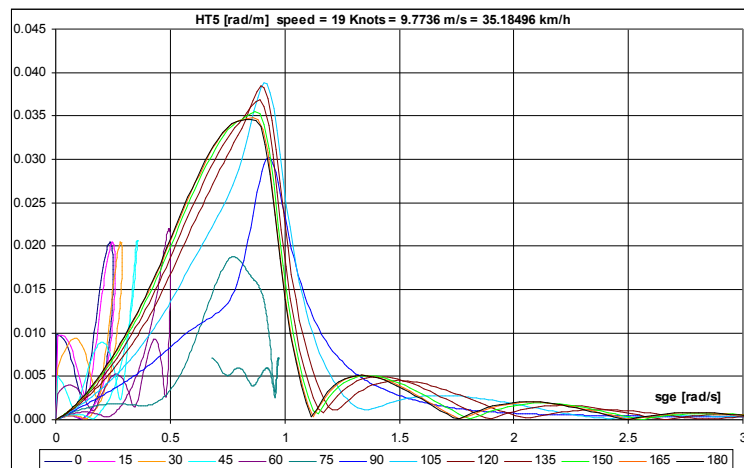


Fig. 5b. Pitch transfer function H_{T3} [m/m], $u_s=19$ [kts]

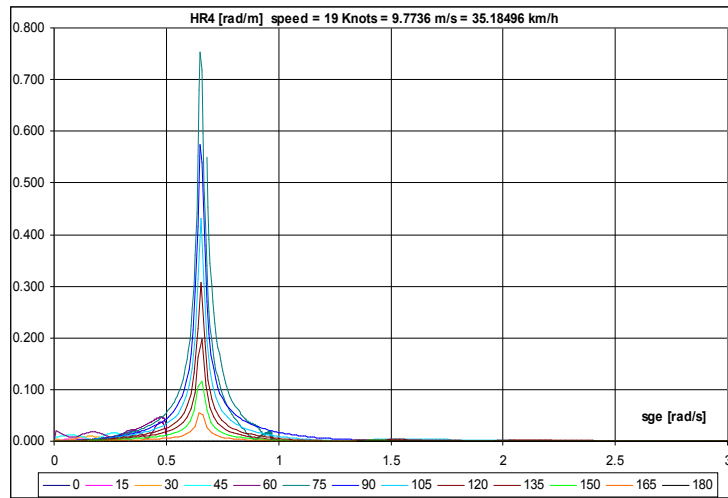


Fig.5c. Roll transfer function H_{R4} [m/m], $u_s=19$ [kts]

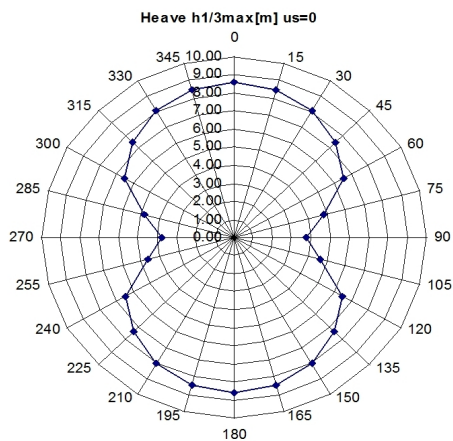


Fig. 6a. Heave $h_{1/3}$ [m] polar diagram, $u_s=0$ [kts]

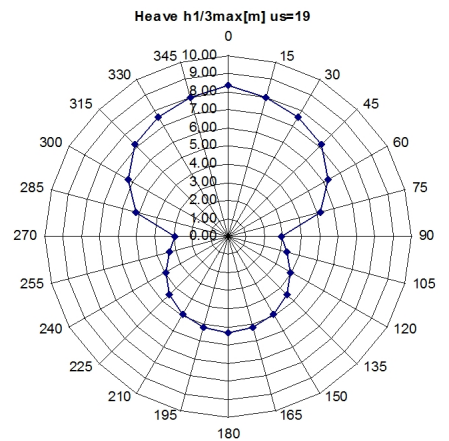


Fig. 7a. Heave $h_{1/3}$ [m] polar diagram, $u_s=19$ [kts]

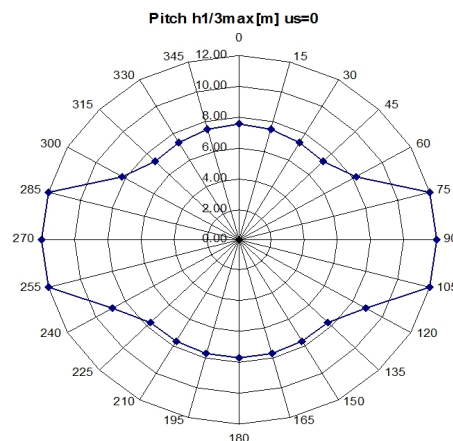


Fig. 6b. Pitch $h_{1/3}$ [m] polar diagram, $u_s=0$ [kts]

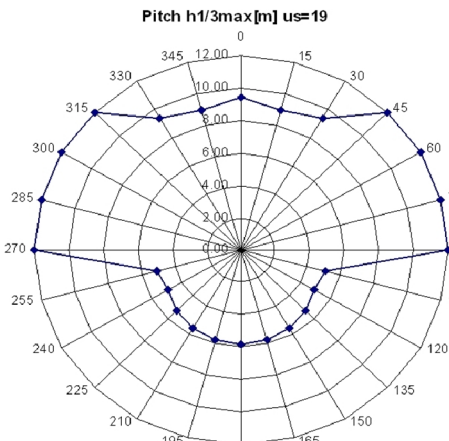


Fig. 7b. Pitch $h_{1/3}$ [m] polar diagram, $u_s=19$ [kts]

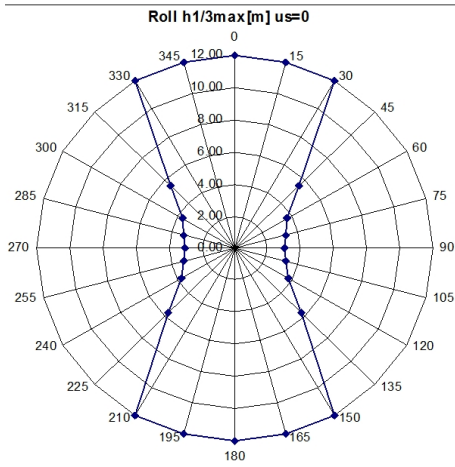


Fig. 6c. Roll $h_{1/3}$ [m] polar diagram, $us=0$ [kts]

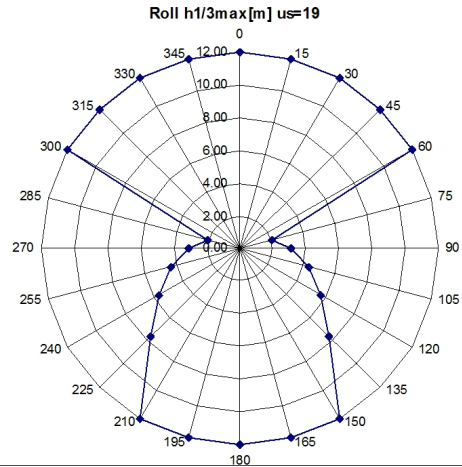


Fig. 7c. Roll $h_{1/3}$ [m] polar diagram, $us=19$ [kts]

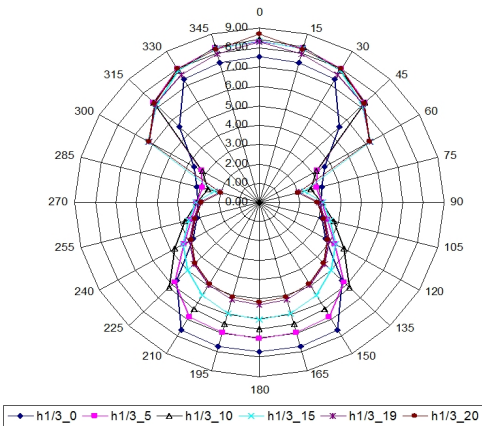


Fig. 8a. Cumulative $h_{1/3}$ [m] polar diagram $us=0-19$ [kts]

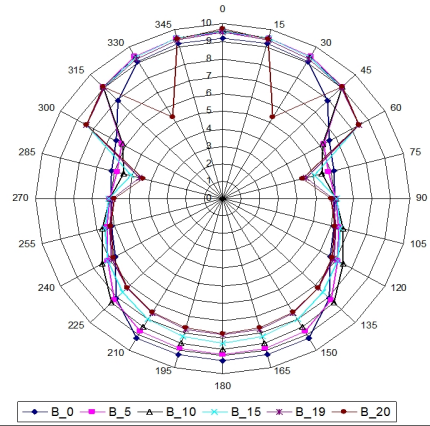


Fig. 8b. Cumulative Beaufort polar diagram $us=0-19$ [kts]

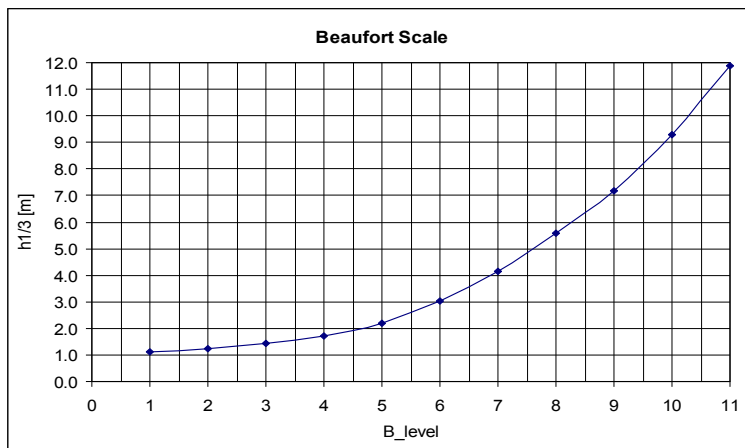


Fig. 8c. The correlation diagram between the significant wave height $h_{1/3}$ [m] and the sea state condition expressed in Beaufort level

4. CONCLUDING REMARKS

Based on the numerical results from Section 3, it results the following conclusions.

1. The maximum significant amplitudes for heave are recorded at $\mu=90$ deg., for roll are recorded at $\mu=75$ deg. for the ship speed=5-19kts and at $\mu=90$ deg. for the ship speed=0kts, for pitch are recorded at $\mu=45$ deg. for the ship speed=0kts, at $\mu=135$ deg. for the ship speed=5, 10kts and at $\mu=120$ deg. for the ship speed=15, 19kts (see Tables 3-7).

2. The maximum significant wave height limit $h_{1/3max}$ (polar diagrams Figs.6-8, Tables 3-7) has the following values: heave $2.833 \div 8.701$ m; pitch $4.842 \div 12$ m; roll $1.911 \div 12$ m; so that the most restrictive seakeeping state is recorded on the roll oscillation component.

3. Due to the ship speed increase from 0 to 19 knots, the cumulative polar diagram (Figs.8a,b) becomes asymmetric (for reference axis $\mu=90$ & 270 deg.), so that the cumulative Beaufort level changes at following seas $\mu=0$ (360) deg. from 9.16 to 9.72 and at head seas $\mu=180$ deg. from 7.70 to 9.25. At beam sea $\mu=90$ (270) deg. the cumulative Beaufort level remains unchanged 6, with no ship speed influence, being the most restrictive sea state condition.

REFERENCES

- [1] **McCreight K.K., Stahl R.G.**, 1985, Recent Advances in the Seakeeping Assessment of Ships, *Naval Engineers Journal*, pp. 224-233.
- [2] **Couser P.**, 2009, Seakeeping analysis for preliminary design, Fremantle, Australia: Formation Design Systems.
- [3] **Kadir Sarioz, Ebru Narli**, 2005, Effect of criteria on seakeeping performance assessment, *Ocean Engineering*, 32, pp. 1161-1173.
- [4] **Rubanenco I., Mirciu I., Domnisoru L.**, 2011, Seakeeping numerical analysis in irregular oblique waves for a simplified ship model, *The Annals of "Dunarea de Jos" University of Galati Fascicle XI – Shipbuilding*, pp. 45-50.
- [5] **Bhattacharyya R.**, 1978, Dynamics of marine vehicles, John Wiley & Sons Publication, New York.
- [6] **Domnisoru, L.**, 2001, Ship Dynamics. Oscillations and Vibrations (in Romanian), Technical Publishing House, Bucharest.
- [7] **Adi Maimun, Omar Yaakob, Md. Ahm Kamal, Ng Chee Wei**, 2006, Seakeeping analysis of a fishing vessel operating in Malaysian water, *Jurnal Mekanikal*, no. 22, pp. 103-114.