### SURFACE PROFILING METHOD OF THE DISK CUTTER OF THE FEMALE ROTOR FROM THE SCREW COMPRESSOR COMPONENT

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#### ABSTRACT

The screw compressor rotors are bounded by cylindrical helical surfaces, with constant pitch. The generation of these surfaces is possible to be done using disk cutter, whose peripheral surfaces are revolution surfaces.

This paper proposes a method and an algorithm for profiling primary surfaces of the disk cutter, mutually enveloping with the helical surfaces of the rotor of the screw compressor.

The algorithm proposes the substitution of the transverse profiles of the rotor by Bézier polynomials.

**KEYWORDS:** helical surfaces, Bézier polynomial, meshing surfaces, disk cutter

#### **1. Introduction**

The profiling problem of disk cutter, tools bounded with revolution surfaces, is according to fundamental theorems of enveloping surfaces.

In some situations, such as screw compressor rotors, due to the complexity of the shape and of the parametric equations, the shape to be obtained is difficult to handle.

The frontal profile of the rotors to be generated using the rack generating, can be realized by the envelope method.

#### 2. The profile generation of the disk cutter

The helical surfaces of screw compressors, male and female, are cylindrical helical surfaces with constant pitch.

Generating these types of surfaces is achieved by milling (grinding) with tools bounded by surfaces of revolution like disk cutter type, Figure 1.

Coordinates systems are defined:

• *XYZ* is the relative system to which is defined the surface of the helicoidal lobe to be generated (Z axis superposed to the rotor axis  $\vec{V}$ );

•  $X_s Y_s Z_s$  - global system associated to disk cutter ( $Z_s$  axis superposed of the disc cutter axis  $\vec{A}$  ).

The axes  $\vec{A}$  and  $\vec{V}$  admit as common perpendicular the axis X (X<sub>s</sub>). The distance between the two axes,  $\vec{V}$  and  $\vec{A}$ , is denoted by *a*.

It is also noted  $\alpha$  the angle between the axes Z and  $Z_s$ , see Figure 1.

Kinematics generation process involves the following movements:

• *I*, *II* - the movement of the helical screw workpiece to be generated, defined by helical parameter  $p_1$  and axis  $\vec{V}$ , for the male rotor (right helix), respectively,  $p_2$  female rotor (left helix);

• *III* - the rotation of disk cutter (cutting movement).

The peripheral surface of the disk cutter is determined as an envelope to each helical rotor to be generated.

The helical surfaces of the female rotor can be known by:

- direct measurement of the points on the generator, performed on a 3D measuring machine, if there is a physical rotor;

- the analytical forms of the rotor composite generator;

-the substitution of the generators rotor, in cross section, by Bézier polynomials of inferior degree, generated through a known small number of points (3 or 4 points).

# 3. Helical surfaces of the female rotor lobes

It is considered that the transverse profile of rotors is the result of enveloping with generating rack (the shape of the generating rack satisfies the specific requirements of a screw compressor rotor construction: no singular points on the profile, asymmetry of the profile generator, meshing line closed and with minimum length).



**Fig. 1.** *The relative position of the rotor and disk cutter to be generated* 

In Figure 2, is given the shape of the transverse profile of the generating rack, whose envelope is the cross section of the screw compressor rotors.

The selection of the generating rack should lead to forms in cross sections of the screw compressor rotor capable to ensure:

- a pronounced asymmetry of the profile shape in order to obtain a satisfactory flow [9];

- a closed meshing line between the compressor rotors in order to ensure the sealing in the compression chambers [9];

- a volume embedded between rotor lobes as low as possible;

- the absence of singular points on the transverse profiles;

- a better processing of the screw compressor rotors, by providing tools for generating profiles without discontinuities [8].

To define a complex profile of the generating rack, which consists of a basic set of profiles, see Table 1.



Fig. 2. Crossing profile of the generating rack for generation of the female rotor

### • Determination of transverse profile of the female rotor

Crossing profile of female rotor is presented in Table 1.

Knowing the profile equations as transverse profile of the female rotor surface, can be determined the equations of the rotor lobes flanks, and hence, using one of the fundamental theorems of the enveloping surfaces [1], [2], [3] we can get the profile disk cutter to generate the gap between two successive lobes of the rotor.

However, we can imagine a solution based on tangents method [4], for which, the problem may be easier to apply.

### •The shape of the helical surface substitute for female rotor

It is considered that the helical surface of the screw rotor compressor can be described as a set of cylindrical helical surfaces and constant step, knowing the cross section of the rotor.

Thus, giving the coordinates of a cross section of the female rotor in the form:

$$\mathbf{G} = \begin{vmatrix} \mathbf{X}_{2_{1}} & \mathbf{Y}_{2_{1}} \\ \mathbf{X}_{2_{2}} & \mathbf{Y}_{2_{2}} \\ \vdots & \vdots \\ \mathbf{X}_{2_{n}} & \mathbf{Y}_{2_{n}} \end{vmatrix},$$
(1)

n is large enough.

	Table 1. The analytical model of crossing profile of th		<b>X</b> 7
Sg.	Family of profiles	Meshing condition	Var. param.
ÂB	$\begin{cases} X_{2} = R_{0}\cos(\psi + \phi_{2}) - (R_{r_{2}} + c_{0}) \cdot \cos \phi_{2} - \\ -R_{r_{2}} \cdot \phi_{2} \cdot \sin \phi_{2}; \\ Y_{2} = -R_{0}\sin(\psi + \phi_{2}) + (R_{r_{2}} + c_{0}) \cdot \sin \phi_{2} - \\ -R_{r_{2}} \cdot \phi_{2} \cdot \cos \phi_{2}; \end{cases}$	$\varphi_2 = -\frac{c_0}{R_{r2}} tg\psi$	$\psi_{min}=0;$ $\psi_{max}=$ constructive
BC	$\begin{cases} X_{2} = -usin(\phi_{2} + \psi_{max}) + (\xi_{B} - R_{r_{2}}) \cdot cos\phi_{2} + \\ + (\eta_{B} - R_{r_{2}} \cdot \phi_{2}) \cdot sin\phi_{2}; \\ Y_{2} = -ucos(\phi_{2} + \psi_{max}) - (\xi_{B} - R_{r_{2}}) \cdot sin\phi_{2} + \\ + (\eta_{B} + R_{r_{2}} \cdot \phi_{2}) \cdot cos\phi_{2}; \end{cases}$	$\varphi_{2} = \frac{-\frac{u}{\cos\psi_{max}} + \xi_{B} \cdot tg\psi_{max}}{R_{r_{2}}} - \frac{\eta_{B}}{R_{r_{2}}}$	$u_{min}=0;$ $u_{max}=$ determined $\beta = \frac{\pi}{2} - \psi_{max}$
ĈĐ	$\begin{cases} \mathbf{X}_{2} = -\mathbf{r}_{0}\cos\left(\nu + \boldsymbol{\phi}_{2}\right) + \left(-\mathbf{R}_{r_{2}} + \boldsymbol{\xi}_{0_{1}}\right) \cdot \cos\boldsymbol{\phi}_{2} + \\ + \left(-\mathbf{R}_{r_{2}} \cdot \boldsymbol{\phi}_{2} + \boldsymbol{\eta}_{0_{1}}\right) \cdot \sin\boldsymbol{\phi}_{2}; \\ \mathbf{Y}_{2} = \mathbf{r}_{0}\sin\left(\nu + \boldsymbol{\phi}_{2}\right) - \left(-\mathbf{R}_{r_{2}} + \boldsymbol{\xi}_{0_{1}}\right) \cdot \sin\boldsymbol{\phi}_{2} + \\ + \left(-\mathbf{R}_{r_{2}} \cdot \boldsymbol{\phi}_{2} + \boldsymbol{\eta}_{0_{1}}\right) \cdot \cos\boldsymbol{\phi}_{2}; \end{cases}$	$\phi_2 = \frac{\xi_{01} \cdot tgv + \eta_{01}}{R_{r_2}}$	$\upsilon_{\min}=0;$ $=\frac{\pi}{2}-\beta$ $\upsilon_{\max}=\frac{\pi}{2}-\beta$
ÊF	$ \begin{cases} \mathbf{X}_{2} = -\mathbf{r}_{0} \cdot \cos\left(\mathbf{v}_{1} - \mathbf{\phi}_{2}\right) + \left(-\mathbf{R}_{\mathbf{r}_{2}} + \boldsymbol{\xi}_{0}_{2}\right) \cdot \cos\boldsymbol{\phi}_{2} + \\ + \left(-\mathbf{R}_{\mathbf{r}_{2}} \cdot \mathbf{\phi}_{2} + \boldsymbol{\eta}_{0}_{2}\right) \cdot \sin\boldsymbol{\phi}_{2}; \\ \mathbf{Y}_{2} = -\mathbf{r}_{0} \cdot \sin\left(\mathbf{v}_{1} - \mathbf{\phi}_{2}\right) - \left(-\mathbf{R}_{\mathbf{r}_{2}} + \boldsymbol{\xi}_{0}_{2}\right) \cdot \sin\boldsymbol{\phi}_{2} + \\ + \left(-\mathbf{R}_{\mathbf{r}_{2}} \cdot \mathbf{\phi}_{2} - \boldsymbol{\eta}_{0}_{2}\right) \cdot \cos\boldsymbol{\phi}_{2}; \end{cases} $	$\varphi_2 = \frac{\xi_{0_2} \cdot tgv_1 + \eta_{0_2}}{R_{r_2}}$	$v_{1\min} = 0;$ $v_{1\min} = \frac{\pi}{2} - \beta_1$ $v_{1\max} = \frac{\pi}{2} - \beta_1$
FG	$\begin{cases} X_2 = u_1 \cdot \cos\left(\phi_2 + \beta_1\right) + \left(\xi_F - R_{r_2}\right) \cdot \cos\phi_2 + \\ + \left(\eta_F - R_{r_2} \cdot \phi_2\right) \cdot \sin\phi_2; \\ Y_2 = -u_1 \cdot \cos\left(\phi_2 + \beta_1\right) - \left(\xi_F - R_{r_2}\right) \cdot \sin\phi_2 + \\ + \left(\eta_F - R_{r_2} \cdot \phi_2\right) \cdot \cos\phi_2; \end{cases}$	$\varphi_2 = \frac{-\frac{u_1}{\sin\beta_1} + \xi_F \cdot \operatorname{ctg}\beta_1 + \eta_F}{R_{r_2}}$	u <sub>1min</sub> =0; u <sub>1max</sub> =determ.
ÂĤ	$\begin{cases} \mathbf{X}_{2} = \left(\xi\left(\lambda_{1}\right) + \mathbf{R}_{r_{2}}\right) \cdot \cos\varphi_{2} - \\ -\left(\eta\left(\lambda_{1}\right) - \mathbf{R}_{r2} \cdot \varphi_{2}\right) \cdot \sin\varphi_{2}; \\ \mathbf{Y}_{2} = -\left(\xi\left(\lambda_{1}\right) - \mathbf{R}_{r2}\right) \cdot \sin\varphi_{2} + \\ +\left(\eta\left(\lambda_{1}\right) - \mathbf{R}_{r2} \cdot \varphi_{2}\right) \cdot \cos\varphi_{2} \cdot; \end{cases}$	$\frac{\dot{x}_{2\lambda_{1}}}{\dot{x}_{2\varphi_{2}}} = \frac{\dot{Y}_{2\lambda_{1}}}{\dot{Y}_{2\varphi_{2}}}$	$0 \le \lambda_1 \le 1$
ĜĤ	$\begin{cases} \mathbf{X}_{2} = \left(\xi\left(\lambda_{2}\right) + \mathbf{R}_{r_{2}}\right) \cdot \cos\varphi_{2} - \\ -\left(\eta\left(\lambda_{2}\right) - \mathbf{R}_{r2} \cdot \varphi_{2}\right) \cdot \sin\varphi_{2}; \\ \mathbf{Y}_{2} = -\left(\xi\left(\lambda_{2}\right) - \mathbf{R}_{r2}\right) \cdot \sin\varphi_{2} + \\ +\left(\eta\left(\lambda_{2}\right) - \mathbf{R}_{r2} \cdot \varphi_{2}\right) \cdot \cos\varphi_{2} \cdot; \end{cases}$	$\frac{\dot{\mathbf{X}}_{2\lambda_{2}}}{\dot{\mathbf{X}}_{2\varphi_{2}}} = \frac{\dot{\mathbf{Y}}_{2\lambda_{2}}}{\dot{\mathbf{Y}}_{2\varphi_{2}}}$	$0 \le \lambda_2 \le 1$

**Table 1.** The analytical model of crossing profile of the female rotor

Two adjacent points, the distance *ds*:

$$ds = \sqrt{\left(X_{2i+1} - X_{2i}\right)^2 + \left(Y_{2i+1} - Y_{2i}\right)^2} \le \varepsilon, \quad (2)$$

if ds is sufficiently small,  $\mathcal{E} = 1 \cdot 10^{-2} \dots 1 \cdot 10^{-1}$ , is obtained:

$$tg\beta_{i} = \frac{|Y_{2i+1} - Y_{2i}|}{|X_{2i+1} - X_{2i}|},$$
 (3)

elementary segment slope determined by points  $M_i [X_{2_i}, Y_{2_i}]$  and  $M_{i+1} [X_{2_{i+1}}, Y_{2_{i+1}}]$ , see Figure 3.



Fig. 3. Elementary helical surface; coordinates systems

Thus, elementary segment  $M_iM_{i+1}$  is described by equations as follows:

$$\mathbf{M}_{i}\mathbf{M}_{i+1} \begin{vmatrix} \mathbf{X}_{2} = \mathbf{X}_{2i} + \boldsymbol{\lambda} \cdot \cos\beta_{i}; \\ \mathbf{Y}_{2} = \mathbf{Y}_{2i} + \boldsymbol{\lambda} \cdot \sin\beta_{i}, \end{vmatrix}$$
(4)

 $\lambda_{\min} = 0; \ \lambda_{\max} = ds$ , see (4).

The segment  $M_iM_{i+1}$  tangent has the follow director parameters:

$$\vec{T}_{M_iM_{i+1}} = \cos\beta_i \cdot \vec{i} + \sin\beta_i \cdot \vec{j} .$$
 (5)

**→** 

After replacement we obtain:

$$\vec{N}_{\Sigma} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ -X_{2i} \sin \theta_2 - Y_{2i} \cos \theta_2 & X_{2i} \cos \theta_2 - Y_{2i} \sin \theta_2 & -p_2 \\ \cos \beta_i & \sin \beta_i & 0 \end{vmatrix}$$
(12)

or, the vectorial form, (11),

$$\vec{N}_{\Sigma} = N_{X_{2}}\vec{i} + N_{Y_{2}}\vec{j} + N_{Z_{2}}\vec{k}$$
(13)  
$$\begin{cases} N_{X_{2}} = p_{2}\sin\beta_{i}; \\ N_{Y_{2}} = -p_{2}\cos\beta_{i}; \\ N_{Z_{2}} = \sin\beta_{i}\left[-X_{2i}\sin\theta_{2} - Y_{2i}\cos\theta_{2}\right] - \cos\beta_{i}\left[X_{2i}\cos\theta_{2} - Y_{2i}\sin\theta_{2}\right].$$
(14)

Elementary helical surface is described in the helical motion  $(V, p_2)$  (left helix), as follows:

$$\begin{vmatrix} \mathbf{X}_2 \\ \mathbf{Y}_2 \\ \mathbf{Z}_2 \end{vmatrix} = \boldsymbol{\omega}_3^{\mathsf{T}} \left( \boldsymbol{\theta}_2 \right) \begin{vmatrix} \mathbf{X}_{2i} \\ \mathbf{Y}_{2i} \\ \mathbf{0} \end{vmatrix} + \begin{vmatrix} \mathbf{0} \\ -\mathbf{p}_2 \boldsymbol{\varphi}_2 \end{vmatrix}$$
(6)

or,  

$$\begin{vmatrix} X_2 \\ Y_2 \\ Z_2 \end{vmatrix} = \begin{vmatrix} \cos \theta_2 & -\sin \theta_2 & 0 \\ \sin \theta_2 & \cos \theta_2 & 0 \\ 0 & 0 & 1 \end{vmatrix} \cdot \begin{vmatrix} X_{2i} + \lambda \cos \beta_i \\ Y_{2i} + \lambda \sin \beta_i \\ 0 \end{vmatrix} + \begin{vmatrix} 0 \\ 0 \\ -p_2 \theta_2 \end{vmatrix},$$
(7)

where  $\theta_2$  is a variable parameter, and  $p_2$  – helical parameter.

For  $\lambda {=}0$  (point  $M_i)$  - equations (6) is the helical line:

$$\begin{cases} X_{2} = X_{2i} \cos \theta_{2} - Y_{2i} \sin \theta_{2}; \\ Y_{2} = X_{2i} \sin \theta_{2} + Y_{2i} \cos \theta_{2}; \\ Z_{2} = -p_{2} \theta_{2}. \end{cases}$$
(8)

Thus, the director parameters of the tangent to helical line (8), are calculated as follows,

$$\vec{\mathrm{T}}_{\mathrm{M}_{\mathrm{i}}} = \frac{\mathrm{d}X_2}{\mathrm{d}\theta_2} \vec{\mathrm{i}} + \frac{\mathrm{d}Y_2}{\mathrm{d}\theta_2} \vec{\mathrm{j}} - \mathrm{p}_2 \vec{\mathrm{k}} \,. \tag{9}$$

The director parameters of the tangent to helical line, for the point  $M_i$ , are calculated from (9):

$$\begin{cases} \frac{\mathrm{dX}_2}{\mathrm{d}\theta_2} = -\mathrm{X}_{2\mathrm{i}}\sin\theta_2 - \mathrm{Y}_{2\mathrm{i}}\cos\theta_2;\\ \frac{\mathrm{dY}_2}{\mathrm{d}\theta_2} = -\mathrm{X}_{2\mathrm{i}}\cos\theta_2 - \mathrm{Y}_{2\mathrm{i}}\sin\theta_2;\\ \frac{\mathrm{dZ}_2}{\mathrm{d}\theta_2} = -\mathrm{p}_2. \end{cases}$$
(10)

Normal to the elementary helical surface, can be approximated, taking into account (4)...(9), in the form:

$$\vec{N}_{\Sigma} = \vec{T}_{M_i M_{i+1}} \times \vec{T}_{M_i}$$
 (11)

Knowing the expression of the director parameters of elementary helical surface (14), we can write the meshing condition, Nikolaev [2].

We define:

-the disk cutter axis A,

$$\vec{A} = \sin \alpha \cdot \vec{j} + \cos \alpha \cdot \vec{k} ; \qquad (15)$$
- vector O<sub>2S</sub>,

 $OO_1 = a \cdot i$ . (16)

The amount of a and  $\alpha$  will be constructively defined, that the axis  $\vec{A}$  is perpendicular to the outside helix female rotor,  $(De_2)$ , Figure 3:

$$\tan \alpha = \frac{2\pi p_2}{\pi D_{e_2}} = \frac{2p_2}{D_{e_2}};$$
 (17)

The meshing condition (18) becomes:

$$\left(\vec{\mathbf{N}}, \vec{\mathbf{A}}, \vec{\mathbf{r}}\right) = \begin{vmatrix} (\mathbf{X}_{2i} \cdot \cos\theta_2 - \mathbf{Y}_{2i} \cdot \sin\theta_2 - \mathbf{a}) & (\mathbf{X}_{2i} \cdot \sin\theta_2 + \mathbf{Y}_{2i} \cdot \cos\theta_2 \\ -\mathbf{p}_2 \cdot \sin\theta_i & \mathbf{p}_2 \cdot \cos\theta_i \\ 0 & \sin\alpha \end{vmatrix}$$

$$\mathbf{\epsilon} = (\mathbf{1}\mathbf{x} \cdot \mathbf{10}^{-3})$$

 $E = (1 \times 10^{-5}).$ 

The points that satisfy the basic meshing condition (20) and belonging to the helical surface represent the characteristic curve - the curve of contact between the helical surface and the primary peripheral surface of the disk cutter.

Be

$$X_{2}^{C} = \left\{ X_{2i}^{C} \quad Y_{2i}^{C} \quad Z_{2i}^{C} \right\}^{T}, i=1...m$$
 (21)

the matrix of points on the characteristic curve.

The transformation of coordinates:

$$\begin{cases} X_{2S} = X_{2i}^{C} - a; \\ Y_{2S} = Y_{2i}^{C} \cos \alpha - Z_{2i}^{C} \sin \alpha; \\ Z_{2S} = Y_{2i}^{C} \sin \alpha + Z_{2i}^{C} \cos \alpha, \end{cases}$$
(22)  
i = 1...m.

move the coordinates of characteristic curve in the reference system belonging to the disk cutter,  $X_{2S}Y_{2S}$  $Z_{2S}$ .

The axial section of the disk cutter is obtained from (22), in the form:

$$\begin{cases} H = Z_{2S} \\ R = \sqrt{X_{2S}^2 + Y_{2S}^2} \end{cases}$$
(23)

·First application (screw compressor, ratio 4/6)

-  $p_2$  is the helical parameter;

- *a* is the sum of the size of inner diameter of the rotor to be generated and outer diameter of the generating disk cutter.

The condition for determining the feature of the elementary helical surface is:

$$\left(\vec{N}_{\Sigma}, \vec{A}, \vec{r}_{2}\right) = 0, \qquad (18)$$

where  $r_2$  is the vector from the current point (elementary helical surface) compared to  $O_{2S}$ ;

$$\vec{r}_{2} = \vec{r} - ai;$$
  

$$\vec{r}_{2} = [X_{2i} \cos \theta_{2} - Y_{2i} \sin \theta_{2}]\vec{i} - a \cdot \vec{i} + (19)$$
  

$$+ [X_{2i} \sin \theta_{2} + Y_{2i} \cos \theta_{2}]\vec{j} - p_{2} \cdot \theta_{2} \cdot \vec{k}.$$

$$\begin{vmatrix} -\mathbf{p}_2 \cdot \mathbf{\theta}_2 \\ \left( \mathbf{X}_{2\mathbf{i}} \cdot \cos(\mathbf{\theta}_2 - \mathbf{\beta}_{\mathbf{i}}) + \mathbf{Y}_{2\mathbf{i}} \cdot \sin(\mathbf{\theta}_2 - \mathbf{\beta}_{\mathbf{i}}) \right) \\ \cos \alpha \end{vmatrix} \leq \varepsilon^{(20)}$$

The algorithm solves all areas of elementary helical surfaces, corresponding to all segments AB,  $\overline{BC}$ ,  $\overline{CD}$ ,  $\overline{EF}$ ,  $\overline{FG}$ ,  $\overline{GH}$ ,  $\overline{HA}$ , components of the rotor.

#### NOTE

If the distance between successive points along the generator is considered small enough (see (2)) these can be approximated the basic equations for helical surface case,  $\lambda=0$ . Thus, elementary helical surface is reduced to a helix and the surface generated is seen as a family of helical lines. This approximation significantly reduces the computation effort and processing time, to determine the characteristic curve and the axial section of the tool disk.

The method is applicable to all segments of the arc of a helical surface.

#### 4. Numerical applications

We present two frontal applications, different constructive solutions.

<b>Table 2.</b> The constructive date of th	he reference rack. (see Figure 2)
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$R_0[mm]$	$r_0$ [mm]	u <sub>max</sub> [mm]	$\Psi_{max}[^0]$	$v_{max}[^0]$	$v_{1max}[^0]$	u <sub>1max</sub> [mm]	L <sub>p</sub> [mm]	$c_0[mm]$	Rr <sub>2</sub> [mm]
22.000	1.100	10.300	63.400	63.400	58.285	6.451	50.265	4.000	48.000

Crt.	R[mm]	H[mm]	Crt.	R[mm]	H [mm]	Crt.	R[mm]	Н	Crt.	R[mm]	Н
no.			no.			no.		[mm]	no.		[mm]
1	47.786	-12.790	11	52.575	-10.917	21	57.217	9.849	31	52.136	11.664
2	48.087	-12.370	12	53.092	-10.763	22	56.705	10.022	32	51.631	11.856
3	48.462	-12.227	13	53.610	-10.612	23	56.195	10.196	33	51.128	12.050
4	48.974	-12.055	14	54.129	-10.463	24	55.685	10.373	34	50.625	12.247
5	49.486	-11.886	15	54.648	-10.316	25	55.176	10.551	35	50.123	12.445
6	49.999	-11.719	16	55.168	-10.172	26	54.667	10.732	36	49.623	12.645
7	50.513	-11.554	17	55.688	-10.030	27	54.160	10.914	37	49.123	12.848
8	51.028	-11.392	18	56.210	-9.890	28	53.652	11.099	38	48.625	13.054
9	51.543	-11.231	19	56.731	-9.751	29	53.146	11.285	39	48.136	13.281
10	52.059	-11.073	20	57.253	-9.612	30	52.640	11.473	40	47.813	13.684

 Table 3. The axial profile of disk cutter coordinates of female rotor

[mm]



Fig. 4. Female rotor – the tooth profile of disk cutter

In the Table 3 are described the axial section coordinates of disk cutter for the female rotor.

The flank of female rotor helicoidal surface is a helicoidal cylindrical surface, constant step, left helix, helicoidal parameter  $p_2$  and  $a = R_s + R_{2int}$ .

**Table 4.** The geometrical constructive elements of the female rotor

$Rr_2$ [mm]	48.000
Rint <sub>2</sub> [mm]	26.034
a [mm]	95.032
p <sub>2</sub> [mm]	28.649
R <sub>s</sub> [mm]	68.998
β[°]	59.181

Helical parameters are calculated with equation:

$$_{2} = \left(\frac{360^{\circ}}{300^{\circ} \cdot i} \cdot D_{1}\right) \cdot \frac{1}{2 \cdot \pi}$$
(24)

with i=4/6 or 3/5.

p



Fig. 5. The geometrical constructive elements of female rotor

#### Second application (screw compressor, ratio 3/5)

 $R_0$  [mm]  $r_0$  [mm] u<sub>max</sub>[mm]  $u_{1max}[mm]$  $L_p[mm]$  $c_0[mm]$  $Rr_2[mm]$  $\Psi_{max}[^0]$  $v_{max}[^{0}]$  $v_{1\text{max}}[^0]$ 22.000 2.000 7.045 70.300 70.300 35.054 7.774 62.832 4.000 50.000 Table 6. The axial profile of disk cutter coordinates of female rotor R[mm] Η R Η Crt. R Η Crt. R Η Crt. Crt. no. [mm] [mm] no. [mm] [mm] no. [mm] no. [mm] [mm] 45.609 -9.426 11 60.330 -6.429 21 65.681 4.944 31 50.284 11.476 1 2 45.941 -9.027 12 60.847 -6.263 22 65.265 5.292 32 49.810 11.740 3 12.005 46.450 -8.844 13 61.360 -6.088 23 64.831 5.617 33 49.336 4 -8.743 5.920 12.271 46.983 14 61.869 -5.899 24 64.381 34 48.863 5 47.517 -8.647 62.373 -5.699 63.917 6.201 48.391 15 25 35 12.537 48.051 -8.554 62.872 -5.485 26 63.444 6.466 36 47.919 12.805 6 16 62.960 47.445 7 48.586 -8.465 17 63.364 -5.257 27 6.712 37 13.073 49.122 8 -8.379 18 63.849 -5.013 28 62.469 6.941 38 46.977 13.342 9 49.658 -8.295 19 64.325 -4.753 29 61.970 7.155 39 46.506 13.612 10 50.195 -8.215 20 64.790 -4.475 30 61.466 7.356 40 46.036 13.883

**Table 5.** The constructive data of the reference rack (see Figure 2)



**Fig. 6.** The solid of disk cutter for female rotor



Fig. 7. Female rotor – the tooth profile of disk cutter

In Table 6 are described the axial section coordinates of disk cutter for the female rotor.

The flank of female rotor helicoidal surface, is a helicoidal cylindrical surface, constant step, left helix, helicoidal parameter  $p_2$  and  $a = R_s + R_{2int}$ .

 Table 7. The geometrical constructive elements

 of female rotor

Rr <sub>2</sub> [mm]	50.000
Rint <sub>2</sub> [mm]	27.442
a [mm]	95.436
p <sub>2</sub> [mm]	33.742
R <sub>S</sub> [mm]	67.994
β[°]	67.978



Fig. 8. The geometrical constructive elements of female rotor



Fig. 9. The solid of disk cutter for female rotor

#### 6. Conclusions

It was considered a constructive form of a helical screw compressor female rotor.

Ratios studied were 4/6 and 3/5.

To determine profiles generating disk cutter the method of tangents was applied.

Solid models and the disk cutter were presented.

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#### REFERENCES

[1]. Litvin, F. L., 1989, "Theory of Gearing", NASA RP-1212 (AVSCOM 88-C-035), Washington, D.C.

[2] Oancea, N., Surface generation through winding, Volume I, Fundamental Theorems, 2004, "Dunărea de Jos"University publishing house, ISBN 973-627-106-4; ISBN 973-627-107-2.

[3] Oancea, N., Surface generation through winding, Volume II, Complementary Theorems, 2004, "Dunărea de Jos"University publishing house, ISBN 973-627-106-4, ISBN 973-627-170-6.

[4] Teodor, V. "Contribution to the elaboration of a method for profiling tools-tools which generate by enwrapping", Lambert Academic Publishing, ISBN 978-3-9433-8261-8.

[5] Zhou Z., 1992, "Computer Aided Design of a Twin Rotor Screw Refrigerant Compressor" Proceedings of the 1992 International Compressor Engineering Conference at Purdue, West Lafayette, pp. 457–465.

[6] Litvin, F. L., and Feng, Pin-Hao, 1997, "Computerized Design, Generation, and Simulation of Meshing of Rotors of Screw Compressor".

[7] Stosic N, Smith I. K, and Kovacevic A, 2002: Optimization of Screw Compressor Design, XVI International Compressor Engineering Conference at Purdue, July 2002.

[8] Stosic, N., Mujic, E., Smith, I.K., Kovacevic, A., "Profiling of Screw Compressor Rotors by Use Direct Digital Simulation". International Compressor Engineering Conference at Purdue, July 2008.

[9] Tseng Ching-Huan, "Synthesis and Optimization for Rotor Profiles in Twin RotorScrew Compressors", Journal of Mechanical Design december 2000, Vol. 122 Õ 545.

[10] Stosic, N., Smith, I., Kovacevic, A., "Screw Compressors – Mathematical Modelling and Performance Calculation". Springer, feb. 2005.

[11] Baicu, I., Oancea, N., "Profilarea sculelor prin modelare solida" Editura TEHNICA-INFO, Chişinău, 2002, ISBN 9975-63-172-X.

## Metodă pentru profilarea sculei disc destinate prelucrării rotorului condus din componența compresorului elicoidal

#### -Rezumat-

Rotoarele compresoarelor elicoidale sunt mărginite de suprafețe cilindrice elicoidale de pas constant. Generarea acestor tipuri de suprafețe este posibil a fi realizată utilizând freze disc a căror suprafețe periferice sunt suprafețe de revoluție.

În prezenta lucrare este propusă o metodă și un algoritm pentru profilarea suprafețelor periferice primare ale frezelor disc, reciproc înfășurătoare cu suprafețele elicoidale ale rotoarelor compresorului elicoidal.

Algoritmul propune substituirea ecuațiilor analitice ale profilului compus al secțiunii transversale a rotorului cu polinoame Bezier de grad inferior.